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can be compared with the calculations. Such data are plotted in Fig. 7. It is readily apparent that the experimental data agree more closely with the results obtained by the use of the elasto-plastic model than with those obtained by the use of the fluid model.

Peak particle velocity as a function of distance is shown in Fig. 8 for the case of an aluminum plate hitting a copper target. Again, the results obtained with the elastoplastic model more nearly agree with the experimental data than do the results from the fluid model. This result is obtained for all reasonable representations of the Hugoniot data of aluminum and copper, i.e., different pairs of values of the parameters A and K.



Fig. 8. Peak Particle Velocity in Copper Target Hit by an Aluminum Projectile

## V. Conclusions

The numerical method for calculating shocks developed by von Neumann and Richtmyer [1] has been successfully applied to a problem involving an elastoplastic stress-strain relation. Comparison of the results of the numerical work with the results of experiments shows that elastoplastic behavior of aluminum and copper is required to account for the observed rapid attenuation of shock waves. Present results are valid for stresses up to 0.1 megabar in aluminum and up to 0.15 megabar in copper.

## Acknowledgment

This research was initiated by the Air Force Special Weapons Center under Contract No. AF 29(601)-6040. It was also partially supported by the Advanced Research Projects Agency, and the Air Force Office of Scientific Research under Contract No. AF 49(638)-1086, and by the Defense Atomic Support Agency under Contract No. DA-49-146-XZ-095.

## References

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- 1. von Neumann, J., and R. D. Richtmyer, A method for the numerical calculation of hydrodynamic shocks, J. Appl. Phys., Vol. 21, 1950, pp. 232-237.
- 2. Fife, I. M., R. C. Eng, and D. M. Young, On the numerical solution of the hydrodynamic equations, SIAM Review, Vol. 3, 1961, pp. 298-308.

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- 3. White, M. P. and L. Griffis, The propagation of plasticity in uniaxial compression, J. Appl. Mech., Reprint-Paper No. 48, APM-17, 1948.
- Wood, D. S., On longitudinal waves of elastic-plastic strain in solids, J. Appl. Mech., Vol. 19, 1952, p. 521.
- Morland, L. W., The propagation of plane irrotational waves through an elastoplastic medium, *Phil. Trans. Roy. Soc.*, London, Ser. 251, 1959, pp. 341-383.
- Fowles, G. R., Attenuation of the shock wave produced in a solid by a flying plate, J. Appl. Phys., Vol. 31, 1960, pp. 655-661.
- Curran, D. R., Nonhydrodynamic attenuation of shock waves in aluminum, J. Appl. Phys., Vol. 34, 1963, pp. 2677-2685.
- Erkman, J. O., Hydrodynamic theory and high pressure flow in solids, Technical Summary Report, No. 2, Stanford Res. Inst., Proj. No. PGU-3712, Stanford Research Institute, Menlo Park, California, 1962.
- Rice, M. H., R. G. McQueen, and M. Walsh, Compression of solids by strong compression waves, Solid State Physics, Vol. 6, F. Seitz and D. Turnbull, eds., Academic Press, N. Y., 1958, pp. 1-63.

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